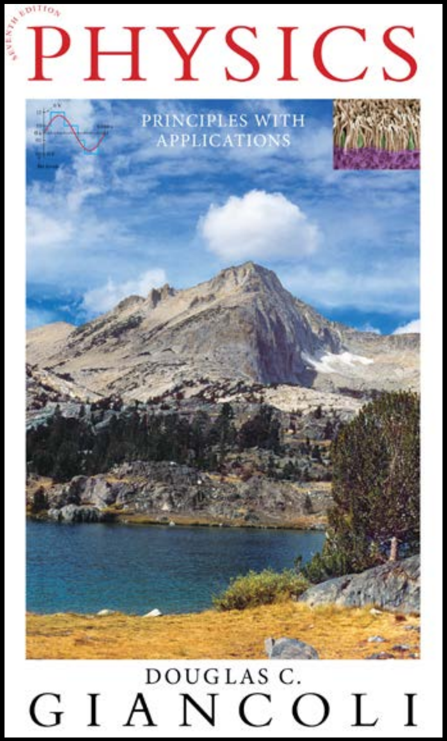

Lecture PowerPoints

Chapter 5
***Physics: Principles with Applications*, 7th edition**
Giancoli

Chapter 5
Circular Motion; Gravitation

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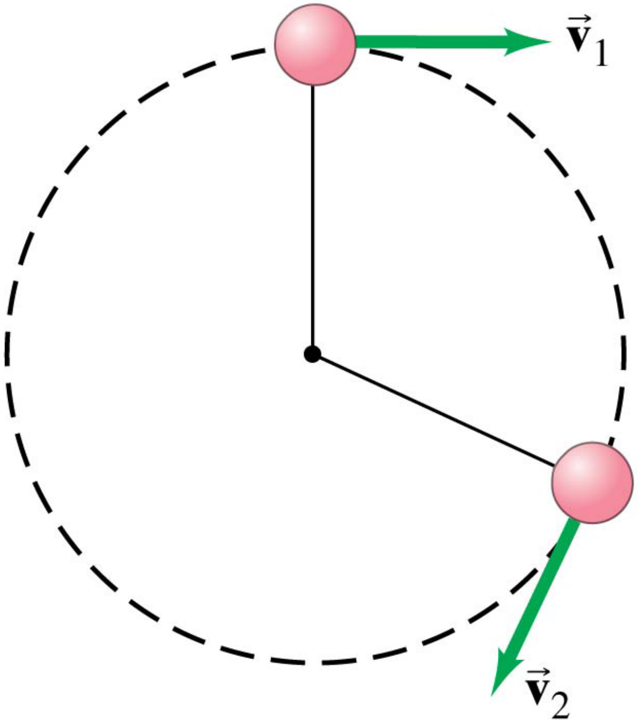
- Planets, Kepler's Laws, the Moon, and Newton's Synthesis
- Types of Forces in Nature

5-1 Kinematics of Uniform Circular Motion

Uniform circular motion: motion in a circle of constant radius at constant speed

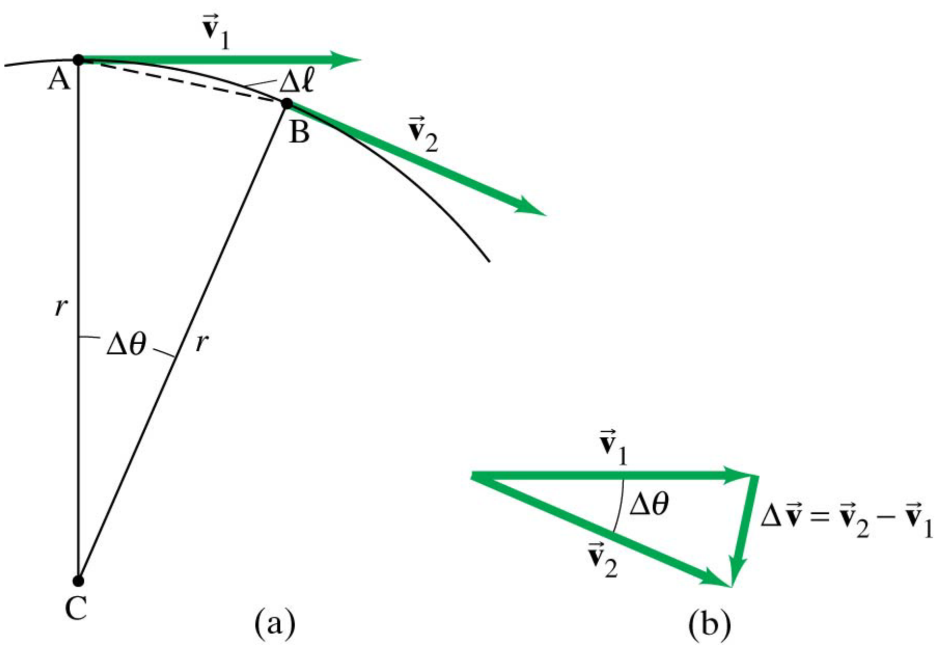
Instantaneous velocity is always tangent to circle.



5-1 Kinematics of Uniform Circular Motion

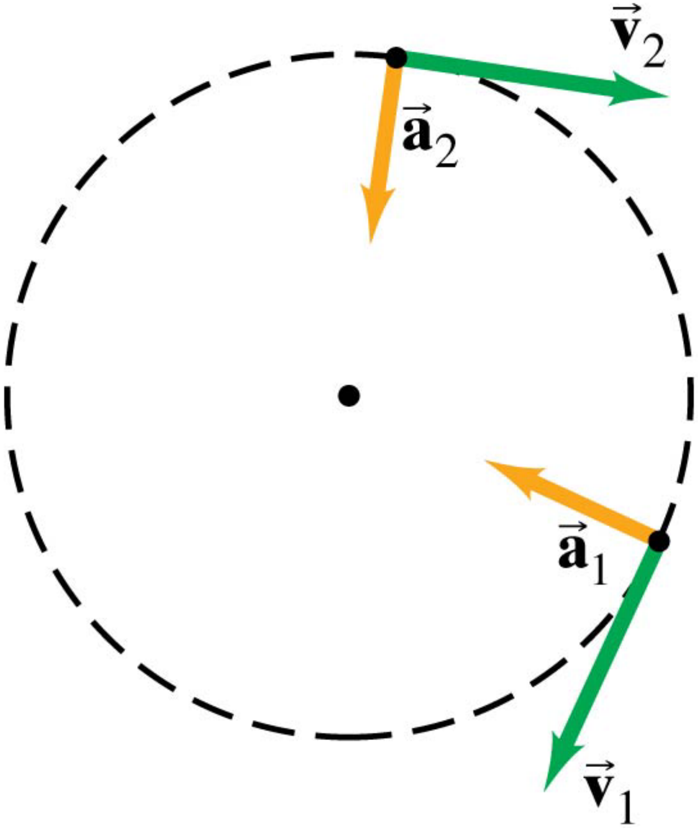
Looking at the change in velocity in the limit that the time interval becomes infinitesimally small, we see that

$$a_R = \frac{v^2}{r}. \qquad (5\text{-}1)$$



5-1 Kinematics of Uniform Circular Motion

This acceleration is called the centripetal, or radial, acceleration, and it points towards the center of the circle.

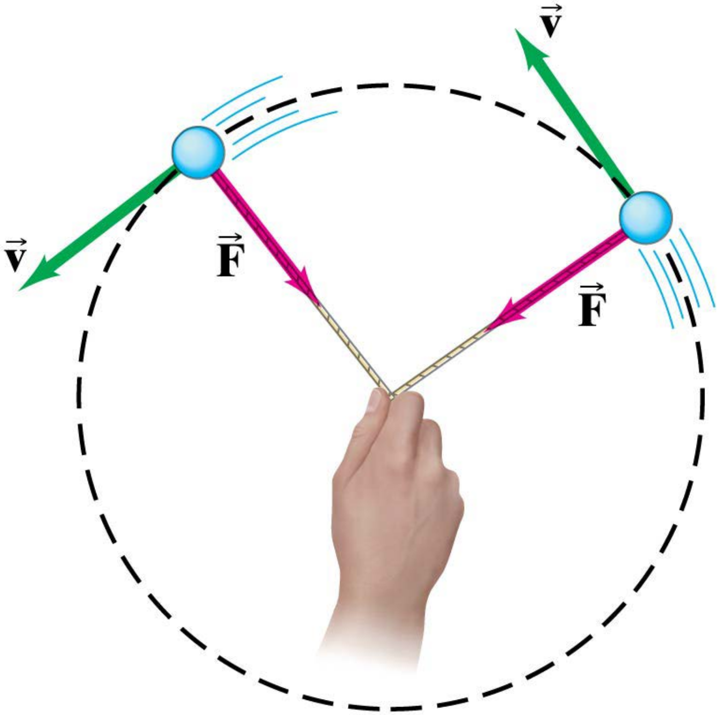


5-2 Dynamics of Uniform Circular Motion

For an object to be in uniform circular motion, there must be a net force acting on it.

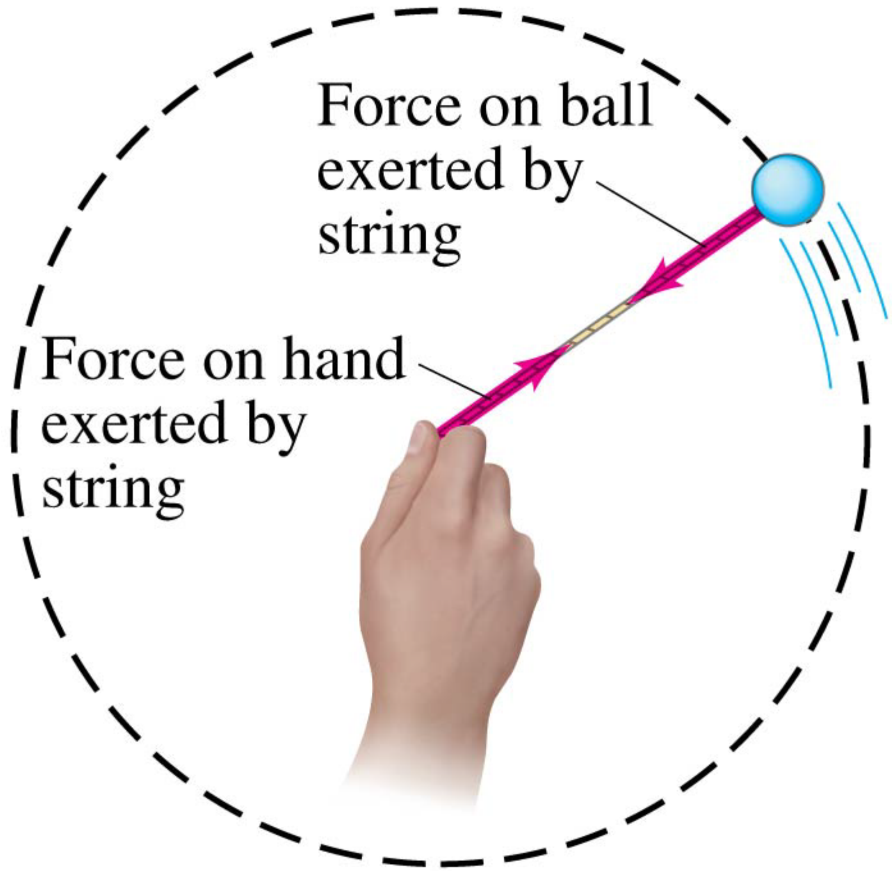
We already know the acceleration, so can immediately write the force:

(5-3) $$\Sigma F_R = ma_R = m\frac{v^2}{r}.$$



5-2 Dynamics of Uniform Circular Motion

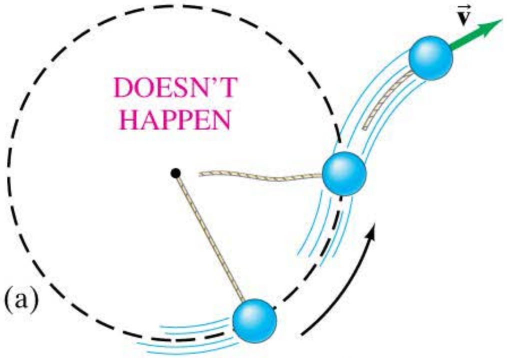
We can see that the force must be inward by thinking about a ball on a string:



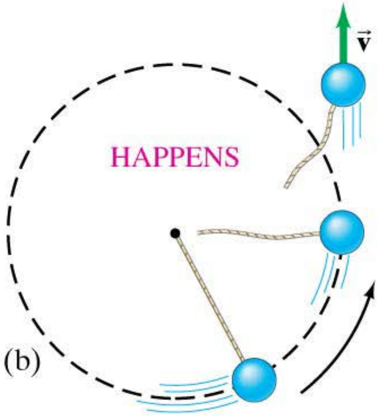
5-2 Dynamics of Uniform Circular Motion

There is no centrifugal force pointing outward; what happens is that the natural tendency of the object to move in a straight line must be overcome.

If the centripetal force vanishes, the object flies off tangent to the circle.



(a)

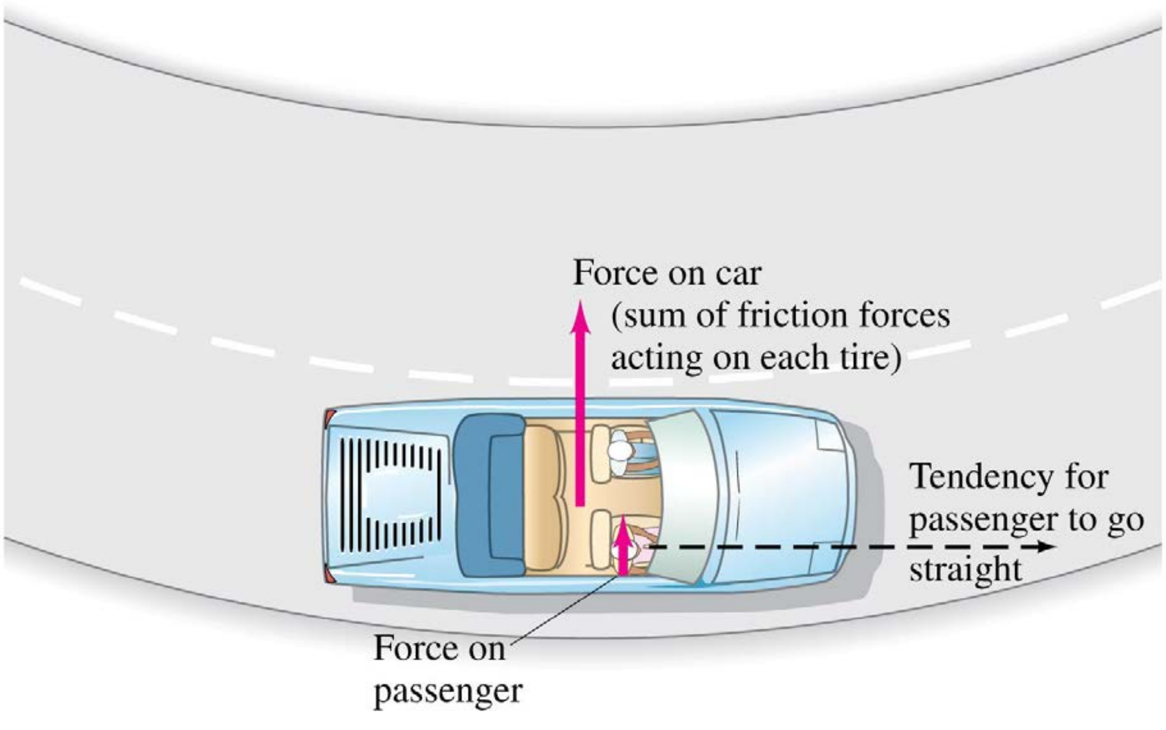


(b)


(c)

5-3 Highway Curves, Banked and Unbanked

When a car goes around a curve, there must be a net force towards the center of the circle of which the curve is an arc. If the road is flat, that force is supplied by friction.



5-3 Highway Curves, Banked and Unbanked

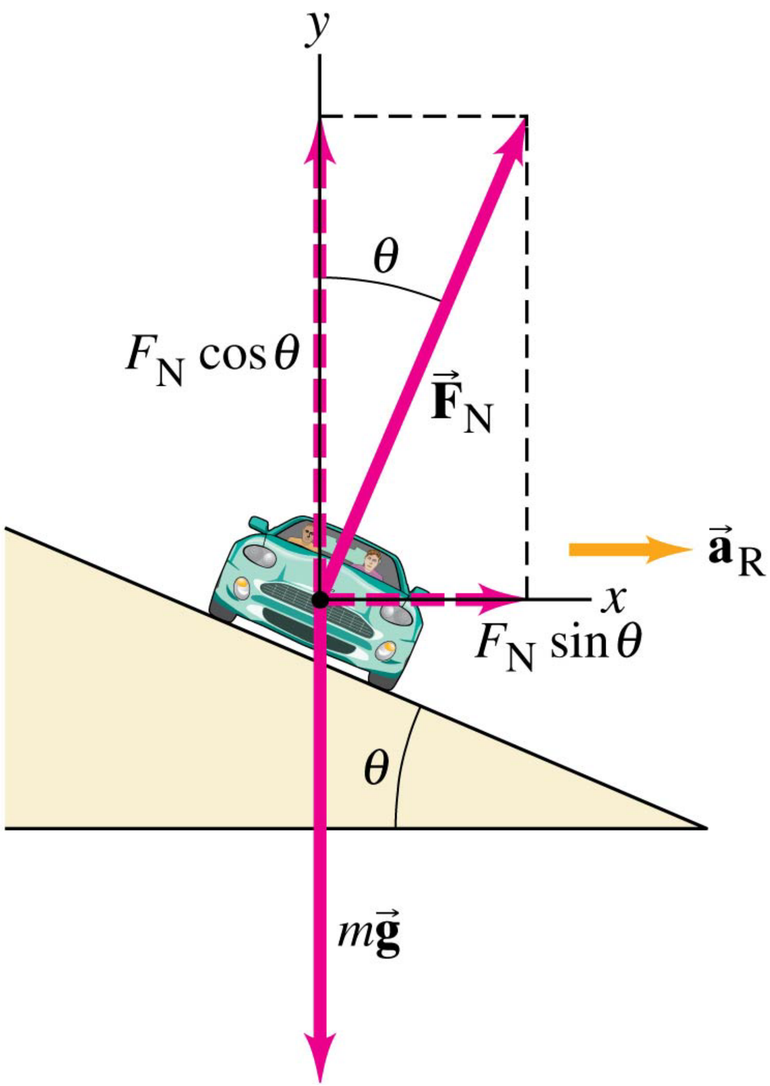
If the frictional force is insufficient, the car will tend to move more nearly in a straight line, as the skid marks show.

5-3 Highway Curves, Banked and Unbanked

As long as the tires do not slip, the friction is static. If the tires do start to slip, the friction is kinetic, which is bad in two ways:

1. The kinetic frictional force is smaller than the static.
2. The static frictional force can point towards the center of the circle, but the kinetic frictional force opposes the direction of motion, making it very difficult to regain control of the car and continue around the curve.

5-3 Highway Curves, Banked and Unbanked

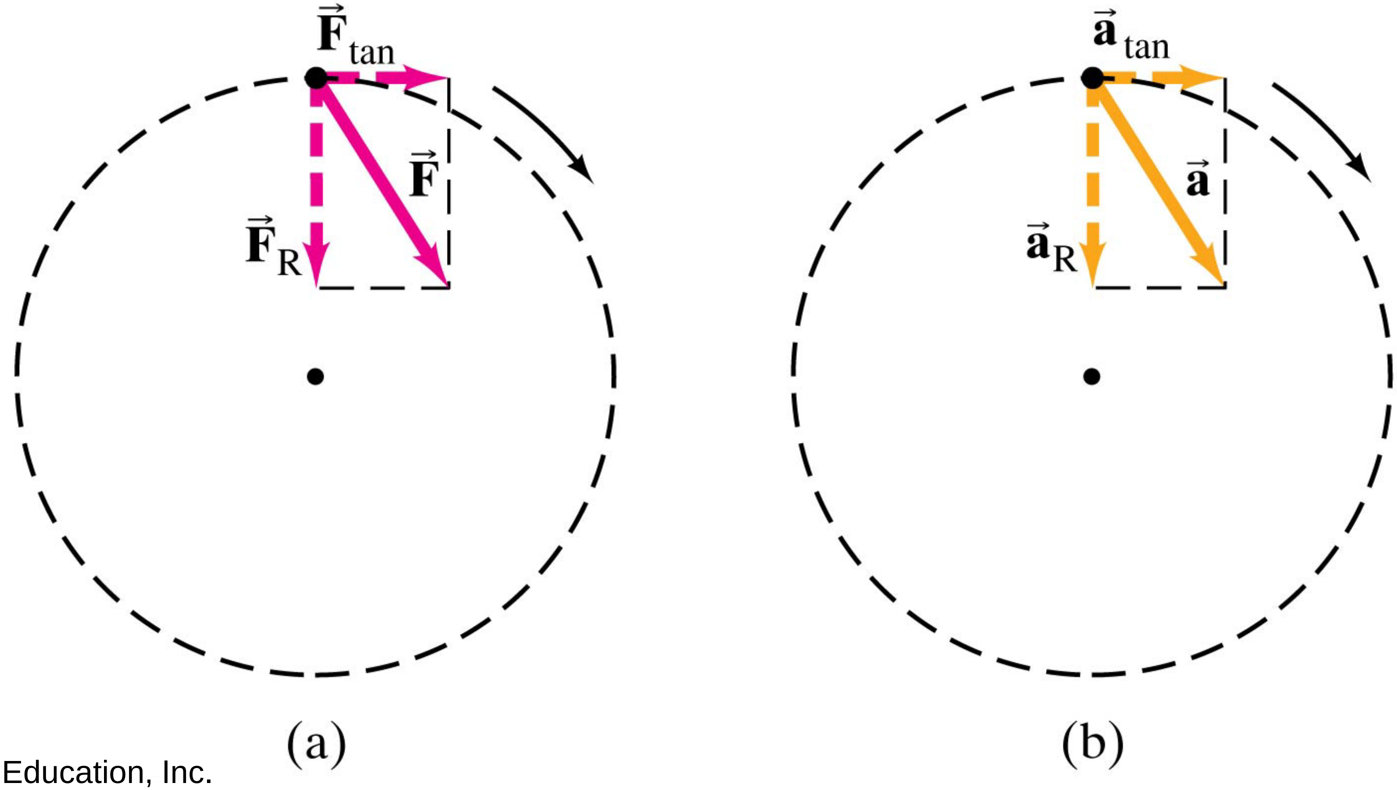


Banking the curve can help keep cars from skidding. In fact, for every banked curve, there is one speed where the entire centripetal force is supplied by the horizontal component of the normal force, and no friction is required. This occurs when:

$$F_N \sin\theta = m\frac{v^2}{r}.$$

5-4 Nonuniform Circular Motion

If an object is moving in a circular path but at varying speeds, it must have a tangential component to its acceleration as well as the radial one.

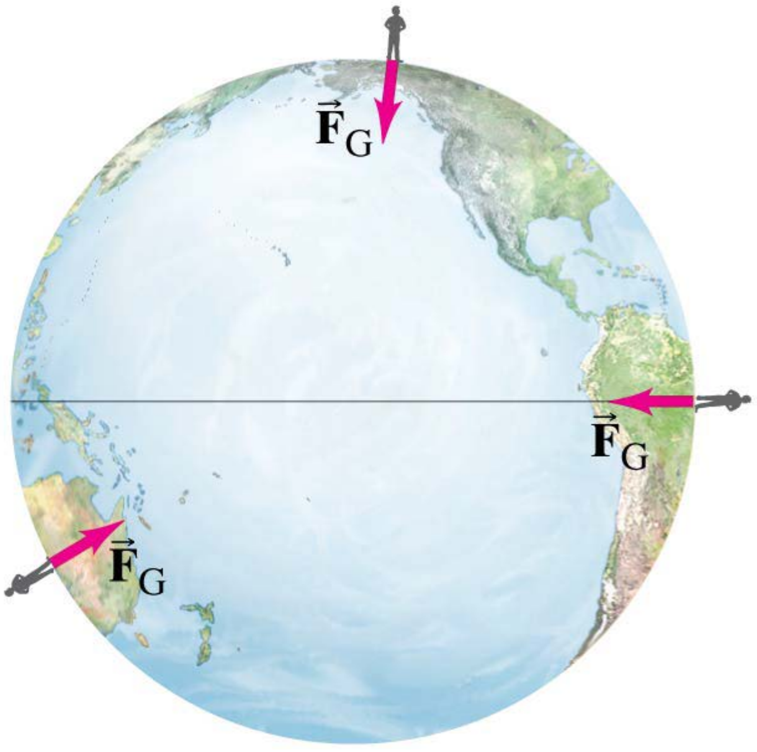


5-5 Newton's Law of Universal Gravitation

If the force of gravity is being exerted on objects on Earth, what is the origin of that force?

Newton's realization was that the force must come from the Earth.

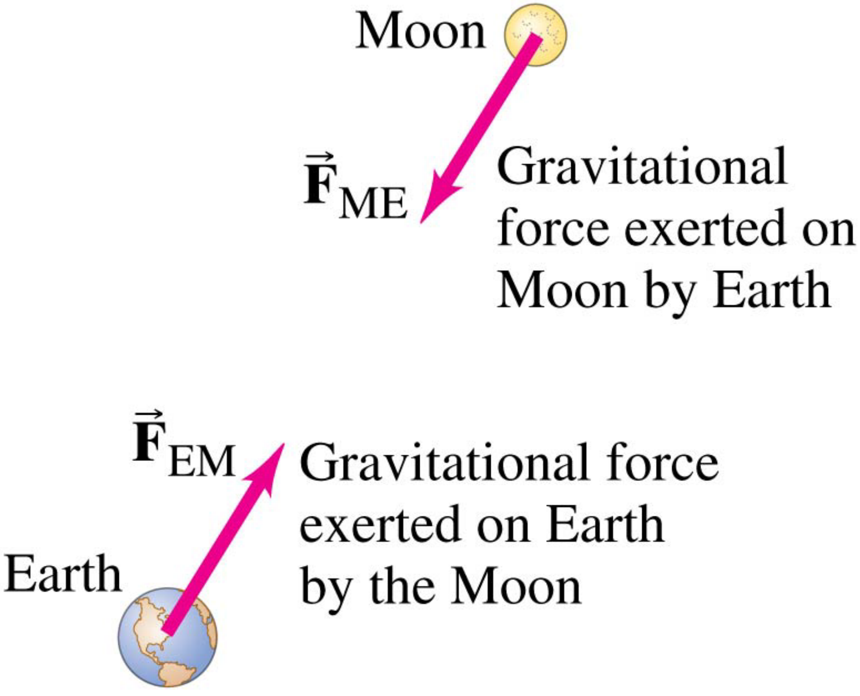
He further realized that this force must be what keeps the Moon in its orbit.



5-5 Newton's Law of Universal Gravitation

The gravitational force on you is one-half of a Third Law pair: the Earth exerts a downward force on you, and you exert an upward force on the Earth.

When there is such a disparity in masses, the reaction force is undetectable, but for bodies more equal in mass it can be significant.



5-5 Newton's Law of Universal Gravitation

Therefore, the gravitational force must be proportional to both masses.

By observing planetary orbits, Newton also concluded that the gravitational force must decrease as the inverse of the square of the distance between the masses.

In its final form, the Law of Universal Gravitation reads:

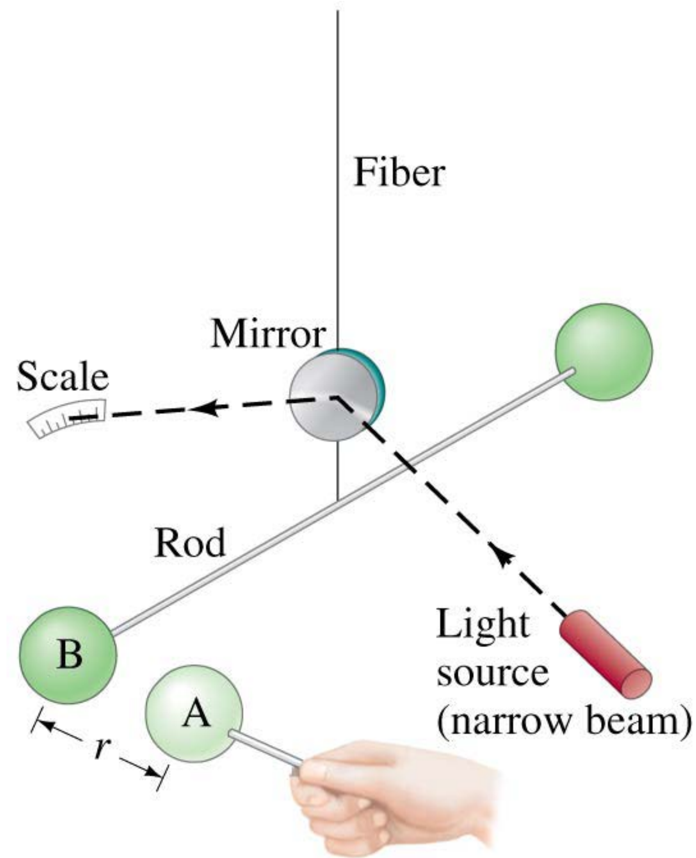
$$F_G = G\frac{m_1 m_2}{r^2}, \qquad (5\text{-}4)$$

where $G = 6.67 \times 10^{-11}\ \mathrm{N{\cdot}m^2/kg^2}$

5-5 Newton's Law of Universal Gravitation

The magnitude of the gravitational constant *G* can be measured in the laboratory.

This is the Cavendish experiment.



5-6 Gravity Near the Earth's Surface

Now we can relate the gravitational constant to the local acceleration of gravity. We know that, on the surface of the Earth:

$$mg = G\frac{mm_E}{r_E^2}.$$

Solving for *g* gives:

$$g = G\frac{m_E}{r_E^2}. \qquad (5\text{-}5)$$

Now, knowing *g* and the radius of the Earth, the mass of the Earth can be calculated:

$$m_E = \frac{gr_E^2}{G} = \frac{(9.80\,\text{m/s}^2)(6.38\times10^6\,\text{m})^2}{6.67\times10^{-11}\,\text{N}\cdot\text{m}^2/\text{kg}^2} = 5.98\times10^{24}\,\text{kg}.$$

5-6 Gravity Near the Earth's Surface

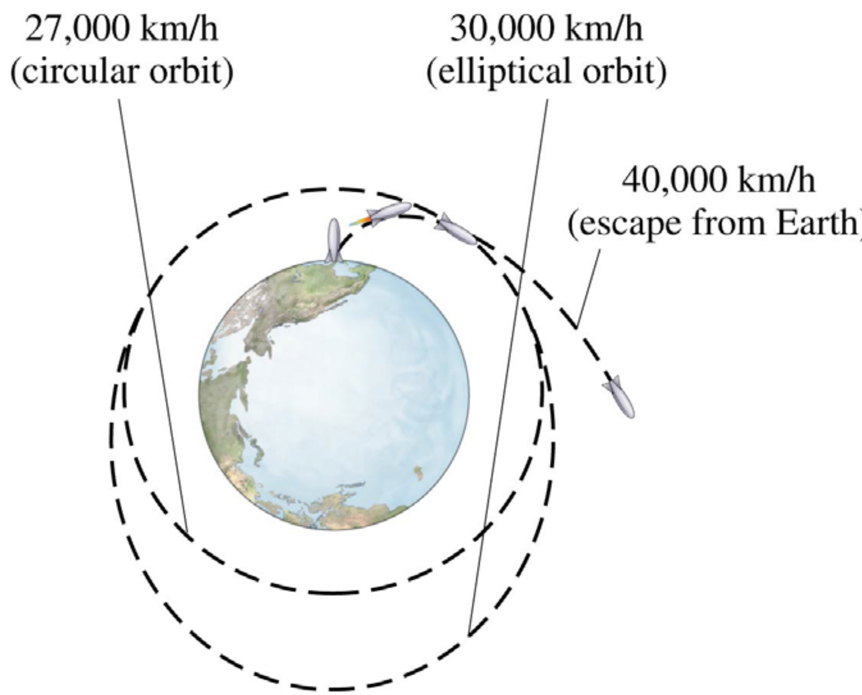
The acceleration due to gravity varies over the Earth's surface due to altitude, local geology, and the shape of the Earth, which is not quite spherical.

TABLE 5–1 Acceleration Due to Gravity at Various Locations

Location	Elevation (m)	g (m/s^2)
New York	0	9.803
San Francisco	0	9.800
Denver	1650	9.796
Pikes Peak	4300	9.789
Sydney, Australia	0	9.798
Equator	0	9.780
North Pole (calculated)	0	9.832

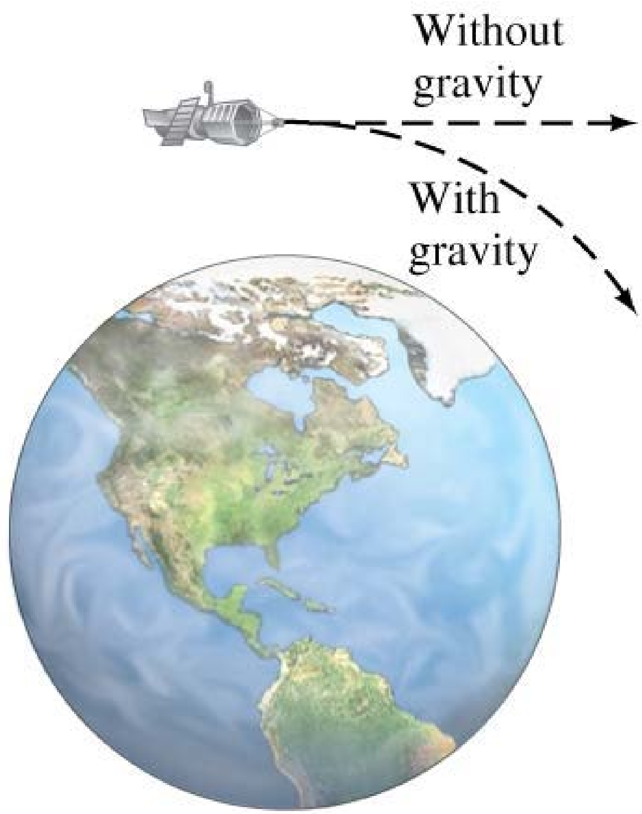
5-7 Satellites and "Weightlessness"

Satellites are routinely put into orbit around the Earth. The tangential speed must be high enough so that the satellite does not return to Earth, but not so high that it escapes Earth's gravity altogether.



5-7 Satellites and "Weightlessness"

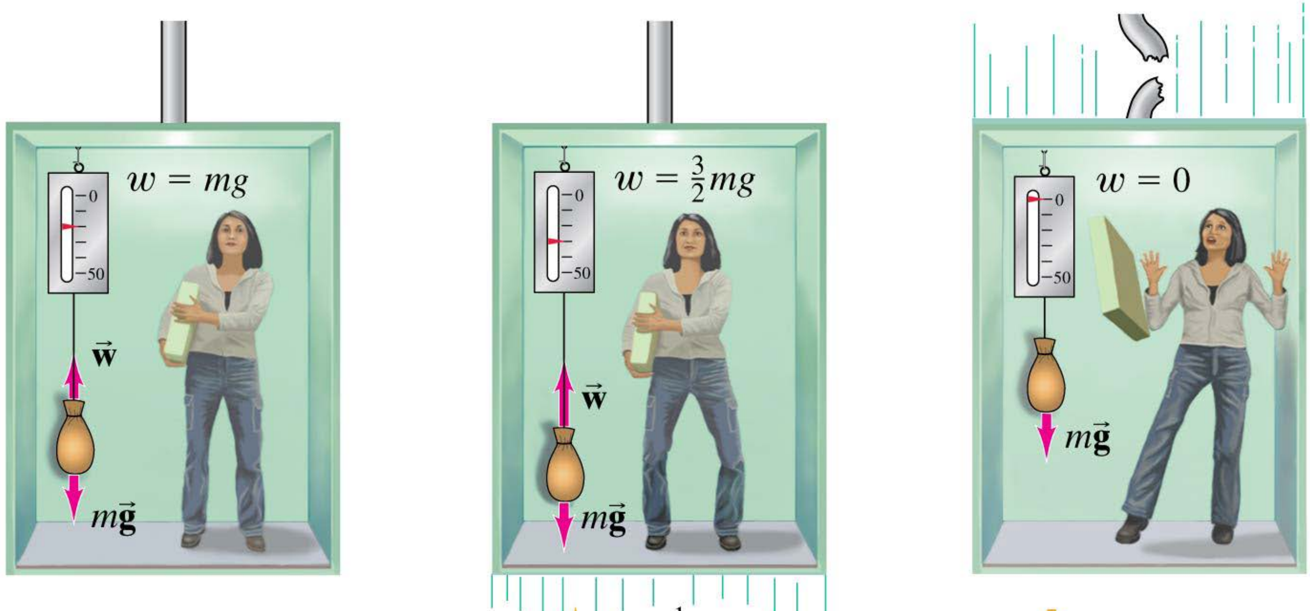
The satellite is kept in orbit by its speed—it is continually falling, but the Earth curves from underneath it.



5-7 Satellites and "Weightlessness"

Objects in orbit are said to experience weightlessness. They do have a gravitational force acting on them, though!

The satellite and all its contents are in free fall, so there is no normal force. This is what leads to the experience of weightlessness.



(a) $a = 0$ (b) $a = \frac{1}{2}g$ (up) (c) $a = g$ (down)

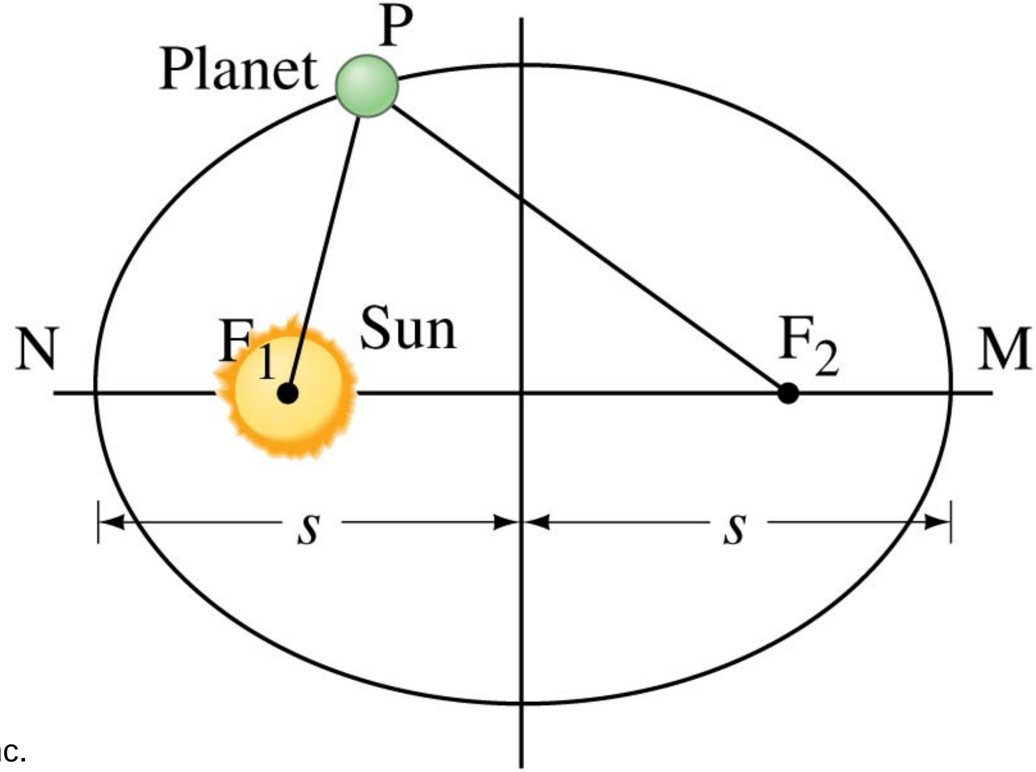
5-7 Satellites and "Weightlessness"

More properly, this effect is called apparent weightlessness, because the gravitational force still exists. It can be experienced on Earth as well, but only briefly:

5-8 Planets, Kepler's Laws, the Moon, and Newton's Synthesis

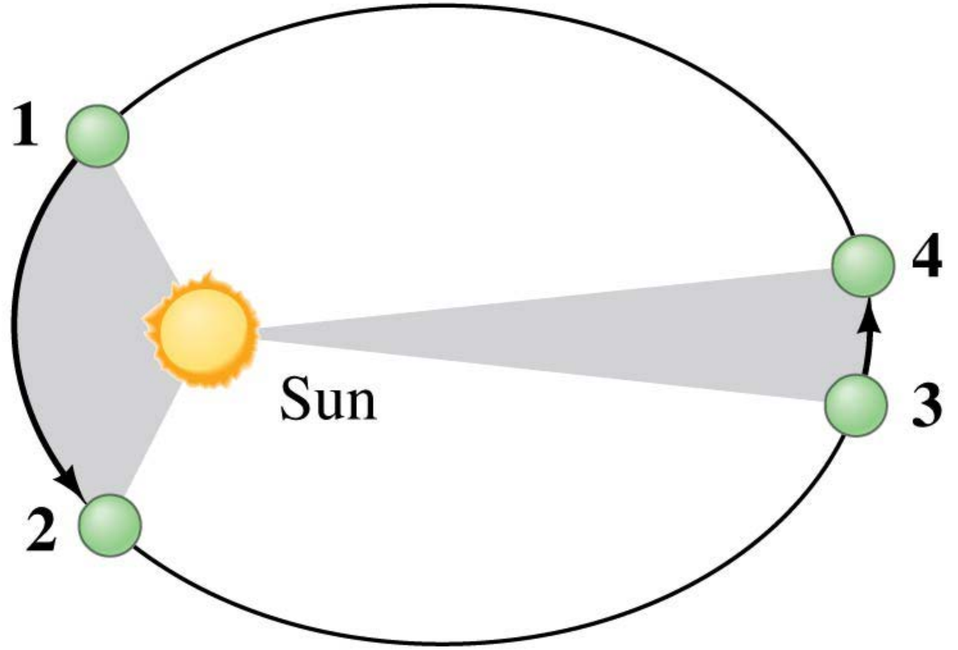
Kepler's laws describe planetary motion.

1. The orbit of each planet is an ellipse, with the Sun at one focus.



5-8 Planets, Kepler's Laws, the Moon, and Newton's Synthesis

2. An imaginary line drawn from each planet to the Sun sweeps out equal areas in equal times.



5-8 Planets, Kepler's Laws, the Moon, and Newton's Synthesis

The ratio of the square of a planet's orbital period is proportional to the cube of its mean distance from the Sun.

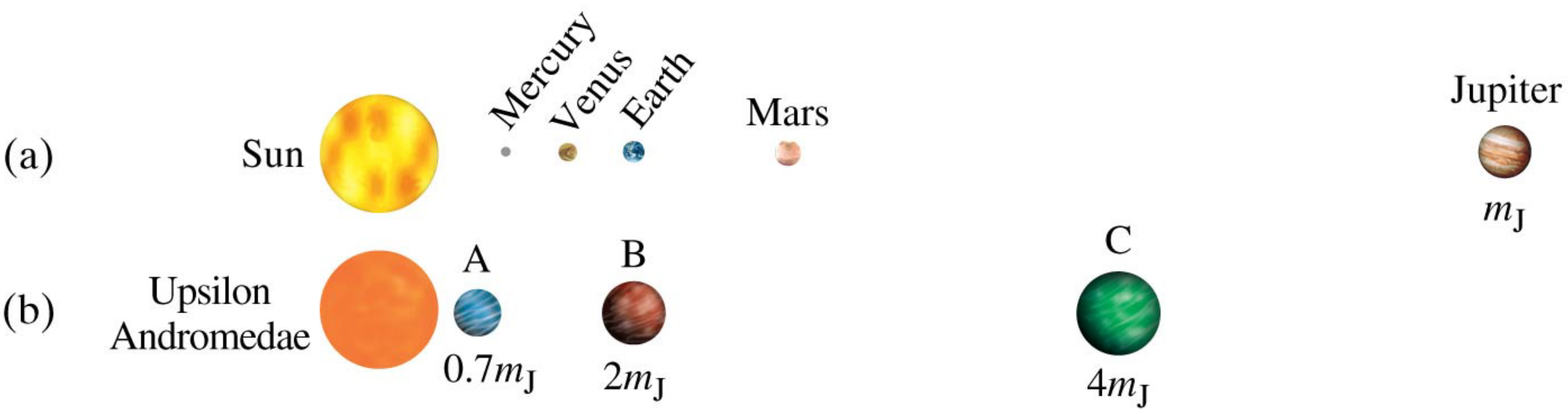
TABLE 5–2 Planetary Data Applied to Kepler's Third Law

Planet	Mean Distance to Sun, s (10^6 km)	Period, T (Earth yr)	s^3/T^2 $\left(10^{24}\,\frac{\text{km}^3}{\text{yr}^2}\right)$
Mercury	57.9	0.241	3.34
Venus	108.2	0.615	3.35
Earth	149.6	1.000	3.35
Mars	227.9	1.88	3.35
Jupiter	778.3	11.86	3.35
Saturn	1427	29.5	3.34
Uranus	2870	84.0	3.35
Neptune	4497	165	3.34
(Pluto)†	5900	248	3.34

†Pluto, since its discovery in 1930, was considered a ninth planet. But its small mass and the recent discovery of other objects beyond Neptune with similar masses has led to calling these smaller objects, including Pluto, "dwarf planets." We keep it in the Table to indicate its great distance, and its consistency with Kepler's third law.

5-8 Planets, Kepler's Laws, the Moon, and Newton's Synthesis

Kepler's laws can be derived from Newton's laws. Irregularities in planetary motion led to the discovery of Neptune, and irregularities in stellar motion have led to the discovery of many planets outside our Solar System.



5-9 Types of Forces in Nature

Modern physics now recognizes four fundamental forces:

1. Gravity
2. Electromagnetism
3. Weak nuclear force (responsible for some types of radioactive decay)
4. Strong nuclear force (binds protons and neutrons together in the nucleus)

5-9 Types of Forces in Nature

So, what about friction, the normal force, tension, and so on?

Except for gravity, the forces we experience every day are due to electromagnetic forces acting at the atomic level.

Summary of Chapter 5

- An object moving in a circle at constant speed is in uniform circular motion.
- It has a centripetal acceleration $a_R = \frac{v^2}{r}$. (5-1)
- There is a centripetal force, which is the mass multiplied by the centripetal acceleration.
- The centripetal force may be provided by friction, gravity, tension, the normal force, or others.

Summary of Chapter 5

- Newton's law of universal gravitation:

$$F_G = G\frac{m_1 m_2}{r^2}, \qquad (5\text{-}4)$$

- Satellites are able to stay in Earth orbit because of their large tangential speed.